

Course Title:

**Material Computation for Structural Geometry**  
**Structural Wood**

Fall 2021

ARCH 732-003

Tuesdays 1:45pm - 4:45pm

Meeting location: MEYH321

Course outline

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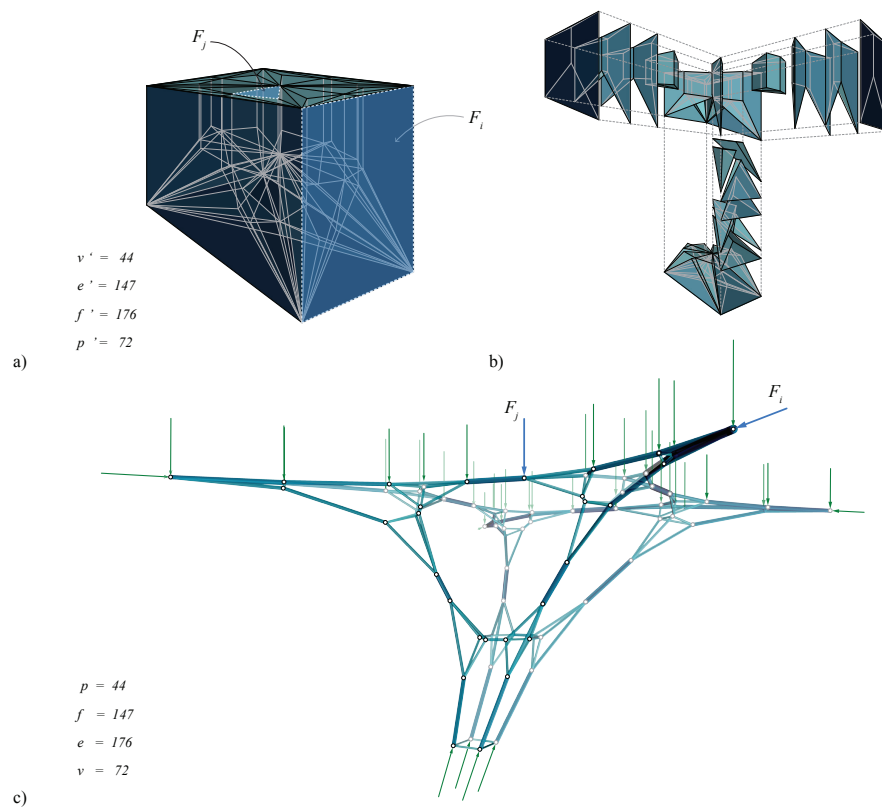


Figure 1: (a) Force diagram consisting of convex polyhedral cells; (b) the exploded axon of the force cells; and (c) the corresponding spatial funicular structural form.

# 1 Course description

*Material Computation for Structural Geometry* course provides a comprehensive introduction to novel geometric methods of structural design based on 2D and 3D graphical statics (Rankine, 1864; Maxwell, 1870; Wolfe, 1921; Akbarzadeh, 2016). The primary emphasis of the course will be on (i) developing a general understanding of the geometric representation of their internal and external equilibrium forces; and (ii) designing material tectonics based on the flow of forces in the system. Considering both force flow and material methods are necessary for designing efficient and innovative architectural structures. This semester, special consideration will be given to structural wood and computational methods for the detail design of joinery and assembly process of spatial node geometry and the proper fabrication techniques to construct the complex geometry of the structure.

Note that this course is based on ongoing research in the field of 3D graphical statics, and therefore provides students with the opportunity to directly contribute to the current research in geometric methods of the structural design. Familiarity with the parametric environment of Grasshopper is required, and code-writing ability is an asset. Particular attention will be given to structural model making and precise structural, architectural and assembly drawings. The outcomes of the course will become a primary collection of Polyhedral Structures Laboratory. Also, a unique summer research fellowship will be available for highly motivated students to build a one-to-one scale structural prototype based on the forms developed in the class.

## 2 Methodology

The course is divided into five consecutive parts with specific intentions; *Part I* will introduce the geometric principles of equilibrium of structural forms (Wolfe, 1921; Akbarzadeh et al., 2015a); *Part II* will focus on structural form finding using geometric techniques (Akbarzadeh et al., 2015c; Lee et al., 2016); *Part III* will concentrate in manipulating the geometry of the structural form and its force diagram to explore various architectural schemes (Akbarzadeh et al., 2015b; Akbarzadeh, 2016); and *Part VI* will specifically emphasize the choice of material and the fabrication techniques to construct complex spatial forms. Table 1 provides a brief overview for each part and its relevant aims and objectives.

### 2.1 Aims

Therefore the course has the following particular intentions:

- to introduce the concept of equilibrium using geometric techniques, expanding the reciprocal relationship between the elements of an equilibrated structural form and its force diagram;
- to emphasize the use of geometry in designing complex yet efficient structural forms and deriving the internal and external forces using geometric diagrams;

<i>Course sections</i>	<i>Aims</i>	<i>Objectives</i>
<i>Part I: the principles of equilibrium</i>	<ul style="list-style-type: none"> <li>• introducing geometric equilibrium of forces in 2D and 3D;</li> <li>• hinting on the properties of form and force diagrams;</li> <li>• defining global and nodal equilibrium;</li> </ul>	<ul style="list-style-type: none"> <li>• to construct parametric form and force diagrams;</li> <li>• to represent different states of equilibrium geometrically;</li> </ul>
<i>Part II: form finding explorations</i>	<ul style="list-style-type: none"> <li>• introducing the technique aggregation in the force diagram;</li> <li>• describing the force subdivision technique;</li> <li>• providing the computational framework for form finding;</li> </ul>	<ul style="list-style-type: none"> <li>• to construct complex structural forms by designing their force diagram;</li> <li>• to produce various structural forms by redistributing the internal forces;</li> </ul>
<i>Part III: manipulating/articulating the design</i>	<ul style="list-style-type: none"> <li>• introducing geometric degrees of freedom of the form and force diagrams;</li> </ul>	<ul style="list-style-type: none"> <li>• iterative design process to fulfill specific architectural needs;</li> </ul>
<i>Part VI: materializing the structural geometry</i>	<ul style="list-style-type: none"> <li>• introducing various materials translating structural geometry into building components;</li> <li>• reviewing multiple fabrication techniques for constructing spatial structural geometry;</li> </ul>	<ul style="list-style-type: none"> <li>• to choose a specific material and translate the structural geometry into a volumetric object based on the properties of the chosen material;</li> <li>• to devise a proper fabrication technique for constructing the structural geometry;</li> </ul>

Table 1: Various parts of the course and their aims and objectives.

- to simplify the understanding of complex structural concepts using geometric language instead of numerical methods; and,
- to investigate different materials and fabrication techniques to realize spatial structural forms .

## 2.2 Objectives

On completion of this course, students should be able to:

- describe the equilibrium of structural concepts using geometric methods of graphical statics in 2D and 3D;
- construct structurally informed, novel architectural concepts and derive the

internal and external forces in the system geometrically; and,

- understand the challenges in materializing spatial structural forms and develop appropriate fabrication techniques to construct their complex components (Jeska and Pascha, 2014; Lennartz and Jacob-Freitag, 2015; Weinand, 2016).

### 3 Grading

Table 2 provides the grading criteria of the course:

<i>Assignment</i>	<i>% of grade</i>	<i>Due date</i>
Session attendance	10	
Exercises	30	Sep 7;21, Oct 5, Oct 19; Nov 5, 19, Nov 2,16,30; Dec 7,14
Physical Prototype	40	Nov 30 – Dec 14
Final structural model	16	Dec 16
Force model	10*	

Table 2: Grading criteria;

\* Additional points for the groups who build their force model for their final projects.

### 4 Lecture schedule

Table 3 represents the schedule as well as the titles of the lectures of the course and their related exercises.

<i>Session Date</i>	<i>Week</i>	<i>Topics</i>
Aug 31	w1	Introduction to geometric methods of structural design
Sep 7	w2	Exercise on a parametric node and its force equilibrium
Sep 14	w3	Compression-only form finding: force subdivision and aggregation
Sep 21	w4	Exercise on compression-only form finding
Sep 28	w5	Compression-and-tension combined systems
Oct 5	w6	Exercise on combined system of forces
Oct 12	w7	Convex hull, Extended Gaussian Image and the data structure of a node
Oct 19	w8	Mid term review: physical structural model and proposition for the building block
Oct 26	w9	Material geometry: computational design workshop
Nov 2	w10	Exercise on section development
Nov 9	w11	Structural performance assessment
Nov 16	w12	Exercise on structural analysis
Nov 23	w13	Assembly techniques and strategies
Nov 30	w14	Exercise on the assembly and part to whole relationship
Dec 7	w15	Progress meeting and preparation for final
Dec 14	w16	Final review

Table 3: Lecture schedule with specific dates for exercises, midterm, and final review dates.

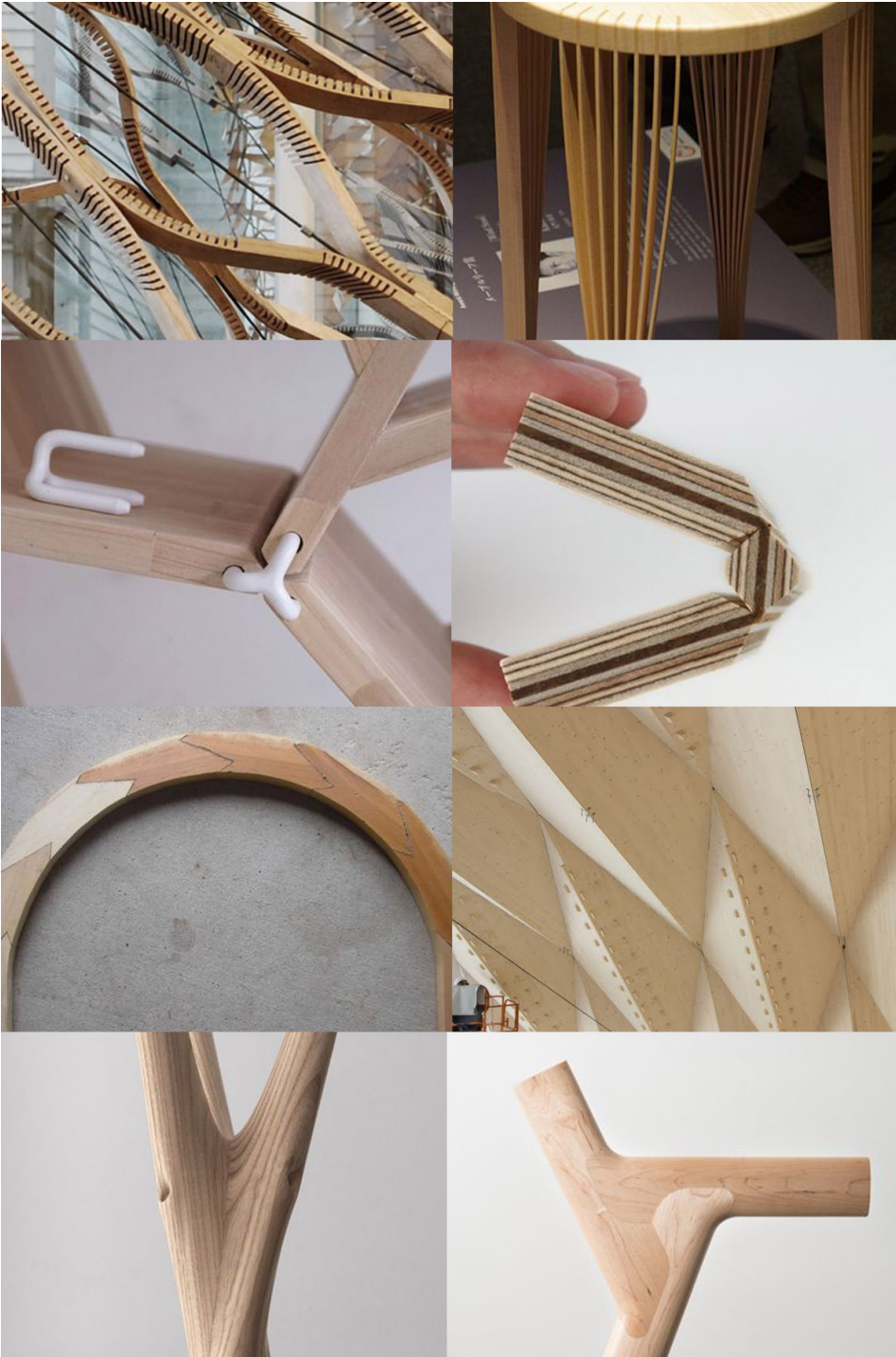


Figure 2: Various joint detailing and fabrication techniques applicable to structural timber.



## References

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